

MCQ

1. An event in the probability that will never be happened is called as.

एक घटना जो कभी नहीं होगी उसे क्या कहा जाता है ?

a) Unsure event b) Sure event
अनिश्चित घटना निश्चित घटना

c) Possible event d) Impossible event
सम्भव घटना असम्भव घटना

2. What will be the probability of getting odd numbers if a dice is thrown ?

एक पासे को फेंकने पर विषम संख्या आने की प्रायिकता क्या होगी ?

a) $\frac{1}{2}$ b) 2
c) $\frac{1}{3}$ d) $\frac{5}{2}$

3. What will be the probability of losing a game if the winning probability is 0.3 ?

यदि एक खेल के जीतने की प्रायिकता 0.3 है तो इसे हारने की प्रायिकता क्या हारी ?

a) 0.5 b) 0.6
c) 0.7 d) 0.8

4. A card is drawn from a pack of 52 cards. What is the probability of getting a king of a black suit ?

52 ताश के पत्तों की एक गड्ढी से एक काला राजा मिलने की प्रायिकता क्या है?

a) $\frac{1}{52}$ b) $\frac{1}{26}$
c) $\frac{3}{26}$ d) $\frac{7}{52}$

5. A card is drawn from a pack of 52 cards. What is the probability of getting a queen card ?

52 ताश के एक गड्ढी से एक पत्ता निकाला गया। उसके रानी होने की प्रायिकता क्या है?

a) $\frac{1}{26}$ b) $\frac{1}{52}$
c) $\frac{3}{13}$ d) $\frac{1}{13}$

6. Which of the following can be the probability of an event ?

निम्न में से कौन सी संख्या किसी घटना की प्रायिकता हो सकती हैं।

a) -1.3 b) 0.4
c) $\frac{3}{8}$ d) $\frac{10}{7}$

7. If $P(A)=\frac{1}{2}$, $P(B)=0$ then $P\left(\frac{A}{B}\right)$ is

यदि $P(A)=\frac{1}{2}$, $P(B)=0$ तब $P\left(\frac{A}{B}\right)$ है।

a) 0 b) $\frac{1}{2}$,
c) Undefined d) 1
परिभाषित नहीं

8. If A and B be two events such that

$P\left(\frac{A}{B}\right)=P\left(\frac{B}{A}\right)\neq 0$, then

यदि A और B दो घटनाएँ इस प्रकार है कि

$P\left(\frac{A}{B}\right)=P\left(\frac{B}{A}\right)\neq 0$, तब
a) $A \subset B$ b) $A=B$
c) $A \cap B \neq \emptyset$ d) $P(A)=P(B)$

9. If E and F are events such that $P(E)=0.6$,

$P(F)=0.3$ and $P(E \cap F) = 0.2$. Find $P\left(\frac{E}{F}\right)$

यदि E और F इस प्रकार की घटनाएँ हैं कि $P(E)=0.6$,

$P(F)=0.3$ और $P(E \cap F) = 0.2$. हैं तो $P\left(\frac{E}{F}\right)$. होगा।

a) $\frac{2}{3}$ b) $\frac{3}{2}$
c) $\frac{1}{6}$ d) $\frac{1}{2}$

10. $P(A \cap B)$ is equal to.

$P(A \cap B)$ के बराबर होगा।

a) $P(A) \cdot P\left(\frac{B}{A}\right)$ b) $P(B) \cdot P\left(\frac{A}{B}\right)$

2 MARKS QUESTION

3 MARKS QUESTION

1. Evaluate $P(A \cup B)$, if $2P(A) = P(B) = \frac{5}{13}$
and $P\left(\frac{A}{B}\right) = \frac{2}{5}$
 $P(A \cup B)$ ज्ञात कीजिए, यदि

$$2P(A) = P(B) = \frac{5}{13} \text{ और } P\left(\frac{A}{B}\right) = \frac{2}{5}.$$

2. Determine $P\left(\frac{E}{F}\right)$ if a coin is tossed three times

Where E: head on third toss & F : head on first two tosses.

$P\left(\frac{E}{F}\right)$ ज्ञात कीजिए । यदि एक सिक्के को तीन बार उछाला गया है, जहाँ E= तीसरी उछाल पर चित फ=पहली दोनो उछालो पर चित ।

3. A family has two children .What is the probability that both the childrens are boys given that at least one of them is a boy?

एक परिवार में दो बच्चे हैं । यदि यह ज्ञात हो कि बच्चों में से कम से कम एक बच्चा लड़का है तो दोनो बच्चों के लड़का होने की क्या प्रायिकता है ?

4. A die is thrown twice and the sum of the numbers appearing is observed to be 6. What is the conditional probability that the number 4 has appeared at least once ?

एक पासे को दो बार उछाला गया और प्रकट हुई संख्याओं का योग 6 पाया गया । संख्या 4 के न्यूनतम एक बार प्रकट होने की सप्रतिबंध प्रायिकता ज्ञात कीजिए ।

5. A fair coin and an unbiased die are tossed .Let A be the event 'head appears on the coin' and B be the event '3 on the die'.Check whether A and B are independent event or not?

एक न्याय्य सिक्का और एक अभिनत पासे को उछाला गया । मान ले A घटना 'सिक्के पर चित प्रकट होता है' और B घटना पासे पर संख्या '3 प्रकट होती है' को निरूपित करते हैं । निरीक्षण कीजिए कि घटनाएँ A और B स्वतंत्र हैं या नहीं?

6. Let A and B be independent events with

$P(A) = 0.3$ and $P(B) = 0.4$ then find

(i) $P(A \cap B)$
(ii) $P(A \cup B)$
(iii) $P\left(\frac{B}{A}\right)$

मान ले A और B स्वतंत्र घटनाएँ हैं तथा $P(A)=0.3$ और $P(B)=0.4$ तब

(i) $P(A \cap B)$

(ii) $P(A \cup B)$

(iii) $P\left(\frac{B}{A}\right)$

ज्ञात कीजिए ।

7. Two balls are drawn at random with replacement from a box containing 10 black and 8 red balls .Find the probability that both balls are red.

दो गेंद एक बॉक्स से बिना प्रतिस्थापित किए निकाली जाती है । बॉक्स में 10 काली और 8 लाल गेंदे हैं तो दोनो गेंदे लाल हाने की प्रायिकता ज्ञात कीजिए ।

5 MARKS QUESTION

1. A bag contains 4 red and 4 black balls, another bag contains 2 red and 6 black balls. One of the two bag is selected at random and a ball is drawn from the bag which is found to be red. Find the probability that the ball is drawn from the first bag.

एक थैले में 4 लाल और 4 काली गेंदे हैं और एक अन्य थैले में 2 लाल और 6 काली गेंदे हैं । दोनो थैलों में से एक को यादृच्छया चुना जाता है और उसमें एक गेंद निकाली जाती है जो लाल है । इस बात की क्या प्रायिकता है कि गेंद पहले थैले से निकाली गई है ?

2. An insurance company insured 2000 scooter driver, 4000 car drivers and 6000 truck drivers. The probability of accident are 0.01, 0.03 and 0.15 respectively. One of the insured persons meets with an accident .What is the probability that he is a scooter driver.

एक बीमा कंपनी 2000 स्कूटर चालकों, 4000 कार चालकों और 6000 ट्रक चालकों का बीमा करती है । दुर्घटनाओं की प्रायिकताएँ क्रमशः 0.01, 0.03 और 0.15 हैं । बीमाकृत व्यक्तियों में से एक दुर्घटनाग्रस्त हो जाता है । उस व्यक्ति के स्कूटर चालक होने की प्रायिकता क्या है ?

3. From a lot of 30 bulbs which include 6 defectives . A sample of 4 bulbs is drawn at random with replacement. Find the probability distribution of the number of defective bulbs.

30 बल्बों के एक ढेर में से 6 बल्ब खराब हैं, 4 बल्बों का एक नमूना (प्रतिदर्शी) यादृच्छया बिना प्रतिस्थापना के निकाला जाता है । खराब बल्बों की संख्या का प्रायिकता बंटन ज्ञात कीजिए ।

4. Find the probability distribution of the number of successive two tosses of a die, where a success is defined as

6. Sol - When a die is thrown, the sample space is

$$S = \{1, 2, 3, 4, 5, 6\}, n(S) = 6$$

let A: the number is even = {2, 4, 6}, $n(A) = 3$

$$\Rightarrow P(A) = \frac{3}{6} = \frac{1}{2}$$

B: the number is red = {1, 2, 3}, $n(B) = 3$

$$\Rightarrow P(B) = \frac{3}{6} = \frac{1}{2}$$

$$A \cap B = \{2\}$$

$$\Rightarrow P(A \cap B) = \frac{1}{6}$$

$$\text{now, } P(A \cap B) = \frac{1}{6}$$

$$\Rightarrow P(A) \cdot P(B) = \frac{1}{6}$$

$$\Rightarrow \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{6}$$

$$\Rightarrow \frac{1}{4} \neq \frac{1}{6}$$

$$P(A) \cdot P(B) \neq P(A \cap B)$$

therefore A and B are not independent event.

7. Sol - Let $P(E_2) = x$; E_1 and E_2 being independent event

$$\therefore P(E_1 \cap E_2) = P(E_1) \cdot P(E_2) = 0.35x$$

$$\Rightarrow P(E_1) + P(E_2) - P(E_1 \cup E_2) = 0.35x$$

$$\Rightarrow 0.35 + x - 0.60 = 0.35x$$

$$\Rightarrow 0.65x = 0.25$$

$$\Rightarrow x = \frac{25}{65} = \frac{5}{13} \text{ Ans}$$

3 MARKS SOLUTION

1.

$$\text{Sol - Given } 2P(A) = P(B) = \frac{5}{13}$$

$$\text{so, } P(A) = \frac{5}{26}$$

$$\& P(B) = \frac{5}{13}$$

$$\text{Also, } P(A/B) = \frac{2}{5}$$

$$\text{We know } P\left(\frac{A}{B}\right) = \frac{P(A \cap B)}{P(B)}$$

$$\therefore P(A \cap B) = P\left(\frac{A}{B}\right) \cdot P(B)$$

$$= \frac{2}{5} \cdot \frac{5}{13}$$

$$= \frac{2}{13}$$

$$\text{Also, } P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$= \frac{5}{26} + \frac{5}{13} - \frac{3}{13}$$

$$= \frac{5 + 10 - 6}{26} = \frac{11}{26} \text{ Ans}$$

2. The sample space of the given experiment will be

$$S = \{\text{HHH, HHT, HTH, THH, HTT, THT, TTH, TTT}\}$$

$$E = \{\text{HHH, HTH, THH, TTH}\}$$

$$F = \{\text{HHH, HHT}\}$$

$$\therefore E \cap F = \{\text{HHH}\}$$

$$\text{so that, } n(S) = 8, n(E) = 4,$$

$$n(F) = 2, n(E \cap F) = 1$$

$$P(E) = \frac{4}{8} = \frac{1}{2}$$

$$P(F) = \frac{2}{8} = \frac{1}{4}$$

$$\text{and } P(E \cap F) = \frac{1}{8}$$

$$\therefore P(E/F) = \frac{P(E \cap F)}{P(F)} = \frac{\frac{1}{8}}{\frac{1}{4}} = \frac{1}{8} \times \frac{4}{1} = \frac{1}{2}$$

3. Sol - Let b stands for boy and g stands for girl.

The sample space of the experiment is

$$S = \{(b, b), (g, b), (b, g), (g, g)\}, n(S) = 4$$

Let E be the event that both children are boys & F is the event that atleast one of the child is a boy,

$$\text{Then, } E = \{(b, b)\} \Rightarrow n(E) = 1$$

$$\& F = \{(b, b), (g, b), (b, g)\} \Rightarrow n(F) = 3$$

$$(E \cap F) = \{(b, b)\} \Rightarrow n(E \cap F) = 1$$

$$\therefore P(E) = \frac{1}{4}, P(F) = \frac{3}{4}, P(E \cap F) = \frac{1}{4}$$

$$\therefore P\left(\frac{E}{F}\right) = \frac{P(E \cap F)}{P(F)} = \frac{\frac{1}{4}}{\frac{3}{4}} = \frac{1}{3}$$

4.

Sol -

The sample space of the given experiment is
 $S = \{(1,1), (1,2), (1,3), \dots, (6,1), (6,2), (6,3), (6,4), (6,5), (6,6)\}$

$$\therefore n(S) = 36$$

Let E be the event that 'number 4 appears at least once' and F be the event that 'the sum of the numbers appearing is 6'.

Then ,

$$E = \{(4,1), (4,2), (4,3), (4,4), (4,5), (4,6), (1,4), (2,4), (3,4), (5,4), (6,4)\}$$

$$\therefore n(E) = 11$$

$$\& F = \{(1,5), (2,4), (3,3), (4,2), (5,1)\}$$

$$\therefore n(F) = 5$$

$$\because (E \cap F) = \{(2,4), (4,2)\} \Rightarrow n(E \cap F) = 2$$

$$\text{Therefore } P(E) = \frac{11}{36}, P(F) = \frac{5}{36},$$

$$P(E \cap F) = \frac{2}{36}$$

\therefore Hence , the required probability

$$P\left(\frac{E}{F}\right) = \frac{P(E \cap F)}{P(F)} = \frac{\frac{2}{36}}{\frac{5}{36}} = \frac{2}{5}$$

5.

Sol - If a fair coin and an unbiased die are tossed, then $S = \{(H,1), (H,2), (H,3), (H,4), (H,5), (H,6), (T,1), (T,2), (T,3), (T,4), (T,5), (T,6)\}$

A = Head appear on the coin

$$= \{(H,1), (H,2), (H,3), (H,4), (H,5), (H,6)\}$$

$$\therefore P(A) = \frac{6}{12} = \frac{1}{2}$$

B = 3 on the die

$$= \{(H,3), (T,3)\}$$

$$\therefore P(B) = \frac{2}{12} = \frac{1}{6}$$

$$\therefore A \cap B = \{(H,3)\}$$

$$P(A \cap B) = \frac{1}{12}$$

Now,

$$P(A) \cdot P(B) = \frac{1}{2} \cdot \frac{1}{6} = \frac{1}{12} = P(A \cap B)$$

\therefore A and B are independent events.

6.

Sol - It is given that

$$P(A) = 0.3 \text{ and } P(B) = 0.4$$

(i) $P(A \cap B) = P(A) \cdot P(B) [\because A \text{ and } B \text{ are independent events}]$

$$= 0.3 \times 0.4 = 0.12 \text{ Ans...}$$

$$(ii) P(A \cup B) = P(A) + P(B) - n(A \cap B)$$

$$= 0.3 + 0.4 - 0.12$$

$$= 0.7 - 0.12$$

$$= 0.58 \text{ Ans...}$$

$$(iii) P\left(\frac{B}{A}\right) = \frac{P(A \cap B)}{P(A)} = \frac{0.12}{0.3} = 0.4 \text{ Ans...}$$

7.

Total number of balls = 18

Number of red balls = 8

Number of black balls = 10

\therefore Probability of getting a red ball in the first draw = $\frac{8}{18} = \frac{4}{9}$

\therefore Probability of getting a red ball in the second draw = $\frac{8}{18} = \frac{4}{9}$

\therefore Probability of getting both balls red = $\frac{4}{9} \times \frac{4}{9} = \frac{16}{81}$

5 MARKS SOLUTION

1. Let E_1 and E_2 be the events of selecting first bag and second bag respectively

$$\therefore P(E_1) = P(E_2) = \frac{1}{2}$$

let A be the event of getting a red ball

$$\therefore P\left(\frac{A}{E_1}\right) = P(\text{drawing a red ball from first bag})$$

$$= \frac{4}{8} = \frac{1}{2}$$

$$\therefore P\left(\frac{A}{E_2}\right) = P(\text{drawing a red ball from second bag})$$

$$= \frac{2}{8} = \frac{1}{4}$$

The probability of drawing a ball from the first bag, given that it is red, is given by $P\left(\frac{E_1}{A}\right)$

[By Baye's theorem]

$$\begin{aligned}\therefore P\left(\frac{E_1}{A}\right) &= \frac{P(E_1) \cdot P\left(\frac{A}{E_1}\right)}{P(E_1) \cdot P\left(\frac{A}{E_1}\right) + P(E_2) \cdot P\left(\frac{A}{E_2}\right)} \\ &= \frac{\frac{1}{2} \cdot \frac{1}{2}}{\frac{1}{2} \cdot \frac{1}{2} + \frac{1}{2} \cdot \frac{1}{4}} = \frac{\frac{1}{4}}{\frac{1}{4} + \frac{1}{8}} = \frac{\frac{1}{4}}{\frac{3}{8}} \\ &= \frac{1}{4} \times \frac{8}{3} = \frac{2}{3} \text{ Ans...}\end{aligned}$$

2.

Sol -

Let E_1 , E_2 and E_3 be the respective events that the drivers are a scooter driver, a car driver and a truck driver.

Let A be the event that the person meets with an accident

$$\begin{aligned}\text{Total no of drivers} &= 2000 + 4000 + 6000 \\ &= 12000\end{aligned}$$

$$\therefore P(E_1) = \frac{2000}{12000} = \frac{1}{6}$$

$$P(E_2) = \frac{4000}{12000} = \frac{1}{3}$$

$$P(E_3) = \frac{6000}{12000} = \frac{1}{2}$$

$$\begin{aligned}P\left(\frac{A}{E_1}\right) &= P(\text{scooter driver meet with an accident}) \\ &= 0.01 = \frac{1}{100}\end{aligned}$$

$$\begin{aligned}P\left(\frac{A}{E_2}\right) &= P(\text{car driver meet with an accident}) \\ &= 0.03 = \frac{3}{100}\end{aligned}$$

$$\begin{aligned}P\left(\frac{A}{E_3}\right) &= P(\text{truck driver meet with an accident}) \\ &= 0.15 = \frac{15}{100}\end{aligned}$$

The probability that the driver is a scooter driver is

$$\begin{aligned}P\left(\frac{E_1}{A}\right) &= \frac{P(E_1) \cdot P\left(\frac{A}{E_1}\right)}{P(E_1) \cdot P\left(\frac{A}{E_1}\right) + P(E_2) \cdot P\left(\frac{A}{E_2}\right) + P(E_3) \cdot P\left(\frac{A}{E_3}\right)} \\ &= \frac{\frac{1}{6} \cdot \frac{1}{100}}{\frac{1}{6} \cdot \frac{1}{100} + \frac{1}{3} \cdot \frac{3}{100} + \frac{1}{2} \cdot \frac{15}{100}} \\ &= \frac{\frac{1}{6}}{\frac{1}{6} + 1 + \frac{1}{2}} = \frac{\frac{1}{6}}{\frac{1+6+45}{6}} \\ &= \frac{1}{6} \times \frac{6}{52} = \frac{1}{52}\end{aligned}$$

3. Sol -

It is given that out of 30 bulbs 6 are defectives.

$$P(\text{defective bulb}) = \frac{1}{5}$$

$$\text{no of non defective bulbs} = 30 - 6 = 24$$

$$P(\text{non - defective bulb}) = \frac{4}{5}$$

4 bulbs are drawn from the lot with replacement.

Let x be the random variable that denotes the number of defective bulbs in the selected bulbs.

$$\therefore P(x = 0) = P(4 - \text{non defective and 0 defective})$$

$$= {}^4C_0 \cdot \left(\frac{1}{5}\right)^0 \left(\frac{4}{5}\right)^4 = \frac{256}{625}$$

$$P(x = 1) = P(3 \text{ non defective and 1 defective})$$

$$= {}^4C_1 \cdot \frac{1}{5} \cdot \left(\frac{4}{5}\right)^3 = \frac{256}{625}$$

$$P(x = 2) = P(2 \text{ non defective and 2 defective})$$

$$= {}^4C_2 \cdot \left(\frac{1}{5}\right)^2 \cdot \left(\frac{4}{5}\right)^2 = \frac{96}{625}$$

$$P(x = 3) = P(1 \text{ non defective and 3 defective})$$

$$= {}^4C_3 \cdot \left(\frac{1}{5}\right)^3 \cdot \frac{4}{5} = \frac{16}{625}$$

$$P(x = 4) = P(0 \text{ non defective and 4 defective})$$

$$= {}^4C_4 \cdot \left(\frac{1}{5}\right)^4 \cdot \left(\frac{4}{5}\right)^0 = \frac{1}{625}$$

hence , the required probability distribution is as follows -

X	0	1	2	3	4
P(x)	$\frac{256}{625}$	$\frac{256}{625}$	$\frac{96}{625}$	$\frac{16}{625}$	$\frac{1}{625}$

4.

Sol -

When a die is tossed two time, we obtain

$$(6 \times 6) = 36 \text{ number of observation,}$$

Let x be the random variable, which represents the number of successes.

(i) Here, success refers to the number greater than 4.

$$P(x = 0) = P(\text{number less than or equal to 4 on both tosses})$$

$$= \frac{4}{6} \cdot \frac{4}{6} = \frac{4}{9}$$

$$\begin{aligned}P(x = 1) &= P\left(\begin{array}{l} \text{number less than or equal to 4 on first toss} \\ \text{and greater than 4 on second toss} \end{array}\right) \\ &+ P\left(\begin{array}{l} \text{number greater than 4 on first toss and} \\ \text{less than or equal to 4 on second toss} \end{array}\right)\end{aligned}$$

$$= \frac{4}{6} \times \frac{2}{6} + \frac{2}{6} \times \frac{4}{6} = \frac{4}{9}$$

$$P(X = 2) = P(\text{number greater than 4 on both the tosses}) \\ = \frac{2}{6} \times \frac{2}{6} = \frac{1}{9}$$

then the probability distribution is as follows -

x	0	1	2
P(x)	$\frac{4}{9}$	$\frac{4}{9}$	$\frac{1}{9}$

(ii) Here, success mean six appears on at least one die

$$P(Y = 0) = P(\text{six does not appear on any of the dice}) \quad 6.$$

$$= \frac{5}{6} \times \frac{5}{6} = \frac{25}{36}$$

$$P(Y = 1) = P(\text{six appears on at least one of the dice})$$

$$= \frac{11}{36}$$

The required probability distribution is as follows

Y	0	1
P(Y)	$\frac{25}{36}$	$\frac{11}{36}$

5.

Sol -

Let x denote the success of getting head .

∴ samle space is

$$S = \{HHH, HHT, HTH, HTT, THH, THT, TTH, TTT\}$$

It can be seen that x can take the value of 0,1,2 or 3.

$$\therefore P(X = 0) = P(TTT) = P(T) \cdot P(T) \cdot P(T) \\ = \frac{1}{2} \cdot \frac{1}{2} \cdot \frac{1}{2} = \frac{1}{8}$$

$$\therefore P(X = 1) = P(HTT) + P(THT) + P(TTH) \\ = \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} + \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} + \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \\ = \frac{3}{8}$$

$$P(X = 2) = P(HHT) + P(HTH) + P(THH) \\ = \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} + \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} + \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} \\ = \frac{3}{8}$$

$$P(X = 3) = P(HHH)$$

$$= \frac{1}{2} \times \frac{1}{2} \times \frac{1}{2} = \frac{1}{8}$$

The required probability distribution is as follows -

X	0	1	2	3
P(X)	$\frac{1}{8}$	$\frac{3}{8}$	$\frac{3}{8}$	$\frac{1}{8}$

$$\text{Means of } X, E(X) = M = \sum X_i P(X_i) \\ = 0 \cdot \frac{1}{8} + 1 \cdot \frac{3}{8} + 2 \cdot \frac{3}{8} + 3 \cdot \frac{1}{8} \\ = \frac{12}{8} = \frac{3}{2}$$

Sol -

Let x denotes the number of balls marked with the digit 0 among the 4 balls drawn. x has a binomial distribution with $n = 4$

$$\text{and } P = \frac{1}{10}$$

$$\therefore q = 1 - \frac{1}{10} = \frac{9}{10}$$

$$\therefore P(X = x) = {}^n C_x q^{n-x} P^x, \quad x = 1, 2, 3, \dots, n$$

$$\therefore P(\text{none marked with 0}) = P(X = 0)$$

$$= {}^4 C_0 \left(\frac{9}{10}\right)^4 \cdot \left(\frac{1}{10}\right)^0 \\ = 1 \cdot \left(\frac{9}{10}\right)^4 = \left(\frac{9}{10}\right)^4$$

Sol -

Let E_1 and E_2 be the respective events of choosing a diamond card and a card which is not diamond.

Let A denote the lost card .

out of 52 cards , 13 cards are diamond and 39 cards are not diamond.

$$\therefore P(E_1) = \frac{13}{52} = \frac{1}{4}, P(E_2) = \frac{39}{52} = \frac{3}{4}$$

When one diamond card is lost -

$$P\left(\frac{A}{E_1}\right) = \frac{{}^{12} C_2}{{}^{51} C_2} = \frac{12!}{2! 10!} \times \frac{2! 49!}{51!} \\ = \frac{11 \times 12}{50 \times 51} = \frac{22}{425}$$

When one card is lost which is not diamond is

$$P\left(\frac{A}{E_2}\right) = \frac{{}^{13} C_2}{{}^{51} C_2} = \frac{13!}{2! 11!} \times \frac{2! 49!}{51!} \\ = \frac{13 \times 12}{50 \times 51} = \frac{26}{425}$$

The probability of getting two cards,
when one card is lost which is not diamond is

$$\begin{aligned}
 P\left(\frac{E_1}{A}\right) &= \frac{P(E_1) \cdot P\left(\frac{A}{E_1}\right)}{P(E_1) \cdot P\left(\frac{A}{E_1}\right) + P(E_2) \cdot P\left(\frac{A}{E_2}\right)} \\
 &= \frac{\frac{1}{4} \cdot \frac{22}{425}}{\frac{1}{4} \cdot \frac{22}{425} + \frac{3}{4} \cdot \frac{26}{425}} \\
 &= \frac{22}{22+78} = \frac{22}{100} = \frac{11}{50} \text{ Ans...}
 \end{aligned}$$

8.

Sol -

Let repeated tossing of the die are

Bernoulli trials.

Let X represents the number of times
of getting sixes in 6 throws of the dice.

Probability of getting six in a single
throw of dice -

$$P = \frac{1}{6}$$

$$\therefore q = 1 - \frac{1}{6} = \frac{5}{6}$$

clearly, X has a binomial distribution

with $n = 6$

$$P(X = x) = {}^n C_x q^{n-x} p^x = {}^6 C_x \left(\frac{5}{6}\right)^{6-x} \left(\frac{1}{6}\right)^x$$

$P(\text{at most 2 sixes}) = P(X \leq 2)$

$$\begin{aligned}
 &= P(X = 0) + P(X = 1) + P(X = 2) \\
 &= {}^6 C_0 \left(\frac{5}{6}\right)^6 \cdot \left(\frac{1}{6}\right)^0 + {}^6 C_1 \left(\frac{5}{6}\right)^5 \cdot \frac{1}{6} + \\
 &\quad {}^6 C_2 \left(\frac{5}{6}\right)^4 \left(\frac{1}{6}\right)^2 \\
 &= \left(\frac{5}{6}\right)^6 + 6 \cdot \left(\frac{5}{6}\right)^5 \cdot \frac{1}{6} + 15 \left(\frac{5}{6}\right)^4 \cdot \frac{1}{36} \\
 &= \left(\frac{5}{6}\right)^4 \left[\frac{25}{36} + \frac{5}{6} + \frac{5}{12} \right] \\
 &= \left(\frac{5}{6}\right)^4 \left[\frac{25 + 30 + 15}{36} \right] \\
 &= \frac{70}{36} \cdot \left(\frac{5}{6}\right)^4 \\
 &= \frac{35}{18} \cdot \left(\frac{5}{6}\right)^4 \text{ Ans....}
 \end{aligned}$$